



## Unit 3: Lesson 01 Inequality statements

Read the symbol,  $>$ , “greater than.”

Read the symbol,  $<$ , “less than.”

If  $a$  lies to the left of  $b$  on a number line, then we can make the statement,  $a < b$ . (Read this, “ $a$  is less than  $b$ .”)

If  $x$  lies to the right of  $y$  on a number line, then we can make the statement,  $x > y$ . (Read this, “ $x$  is greater than  $y$ .”)

Just remember, “The alligator eats the big one.”

**Example 1:** Express “ $x + 3$  is greater than  $2y$ ” in symbols.

$$x + 3 > 2y$$

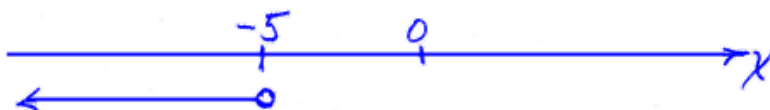
**Example 2:** The number represented by  $m$  lies to the right of the number represented by  $n$  on a number line. Express the inequality relationship between  $m$  and  $n$  using “ $<$ ”.

$$n < m$$

When graphing  $x > a$  or  $x < a$  on a number line just remember that the “inequality arrow” is in the **same direction** as the “graph arrow” (only true when the **variable is on the left side**).

Graph with an **open circle** as illustrated in the example below.

**Example 3:** Sketch the graph of  $x < -5$  on a number line.



Read the symbol,  $\geq$ , “greater than or equal to.”

Read the symbol,  $\leq$ , “less than or equal to.”

Graph with a **solid circle** as illustrated in the example below.

**Example 4:** Sketch the graph of  $x \geq 4$  on a number line.



**Adding** (or subtracting) a number to both sides of an inequality:

Suppose  $a$  and  $b$  are related by the inequality, then

$$a > b$$

When the quantity  $c$  is added to both sides, the result is

$$a + c > b + c$$

**Multiplying** (or dividing) a number times both sides of an inequality:

Suppose  $a$  and  $b$  are related by the inequality, then

$$a > b$$

When the quantity  $c$  is multiplied by both sides, the result is

$$a(c) > b(c) \quad \text{if } c \text{ is a } \mathbf{positive} \text{ number.}$$

$$a(c) < b(c) \quad \text{if } c \text{ is a } \mathbf{negative} \text{ number (Note the } \mathbf{reversal} \text{ of the inequality symbol.)}$$

**Example 5:** Rewrite the inequality  $f < g$  after subtracting 3 from both sides.

$$f - 3 < g - 3$$

**Example 6:** Rewrite the inequality  $m \geq n$  after multiplying 4 times both sides.

$$4m \geq 4n$$

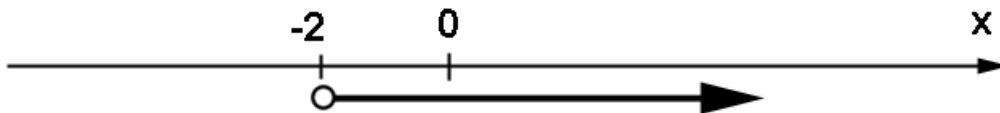
**Example 7:** Rewrite the inequality  $x \geq y$  after dividing both sides by  $-6$ .

$$x/(-6) \leq y/(-6)$$

**Example 8:** Rewrite the inequality  $p \leq q$  after adding 2 to both sides.

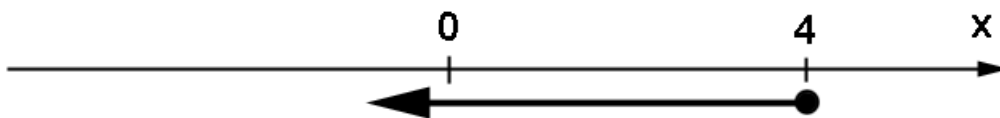
$$p + 2 \leq q + 2$$

**Example 9:** Write the inequality that describes this graph.



$$x > -2$$

**Example 10.** Write the inequality that describes this graph.



$$x \leq 4$$

**Example 11:** Which of the following set of  $x$  values is a solution to the inequality of Example 10?  $\{-6, -5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5, 6\}$

$$\{-6, -5, -4, -3, -2, -1, 0, 1, 2, 3, 4\}$$

**Assignment:**

1. Express “ $f$  is less than or equal to  $m$ ” in mathematical symbols.

2. Express “ $z$  is greater than  $v$ ” in mathematical symbols.

3. Express  $x \leq k$  in words.

4. Express  $w > z$  in words.

5. Rewrite the inequality  $f < g$  after subtracting 3 from both sides.

6. Rewrite the inequality  $x \geq y$  after dividing both sides by  $-6$ .

7. Rewrite the inequality  $m \geq n$  after multiplying 4 times both sides.

8. Rewrite the inequality  $p \leq q$  after adding 2 to both sides.

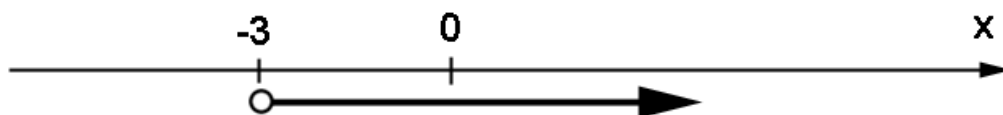
9. Sketch the graph of  $x < 6$  on a number line.

10. Sketch the graph of  $x \geq -7$  on a number line.

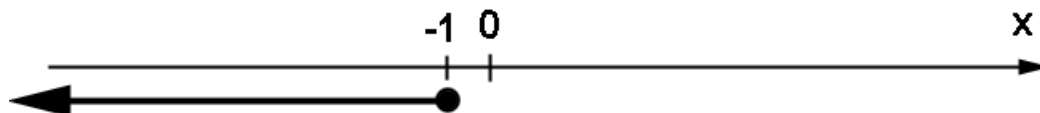
11. Sketch the graph of  $x \geq 2.5$  on a number line.

12. Sketch the graph of  $x < -3$  on a number line.

13. Write the inequality that describes this graph.



14. Write the inequality that describes this graph.



15. Which of the following set of  $x$  values is a solution to the inequality of problem 13?

$\{-5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5\}$

16. Which of the following set of  $x$  values is a solution to the inequality of problem 14?

$\{-5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5\}$

17. Express “ $p$  could be equal to 5; however, it could also be less than 5” in mathematical symbols.

18. Rewrite  $2g \geq 11f$  after dividing both sides by  $-13$ .

19. Express  $m \leq n$  in words.

20. Sketch the graph of  $x < 0$  on a number line.